

Edmonds Karp Algorithm

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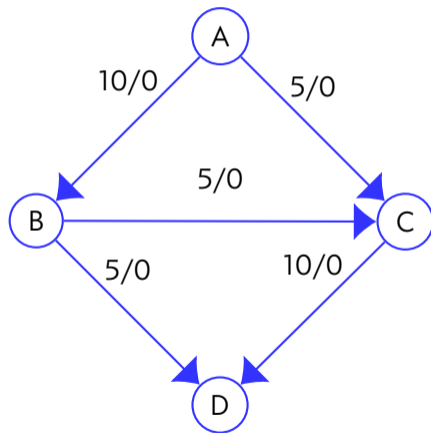
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Objectives

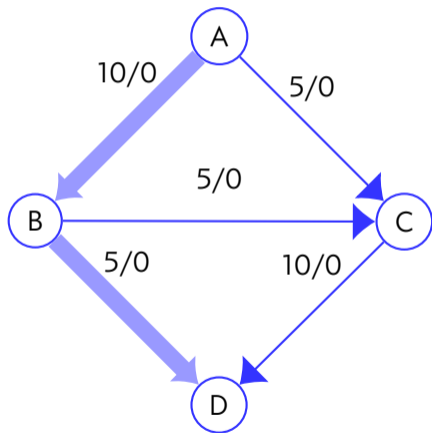
Your Objectives:

- ▶ Implement the Edmonds Karp algorithm for Network Flow

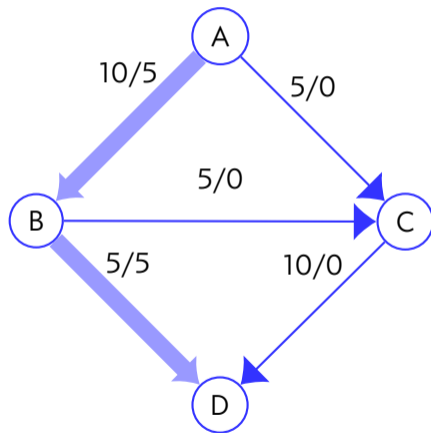
A simple example



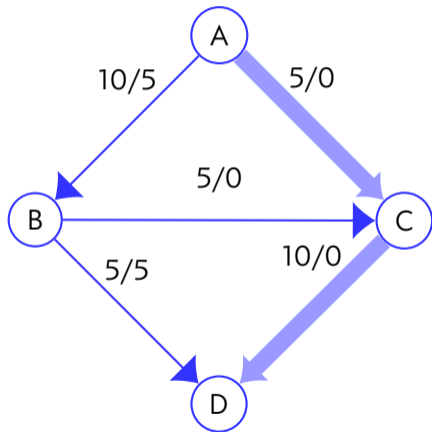
A simple example



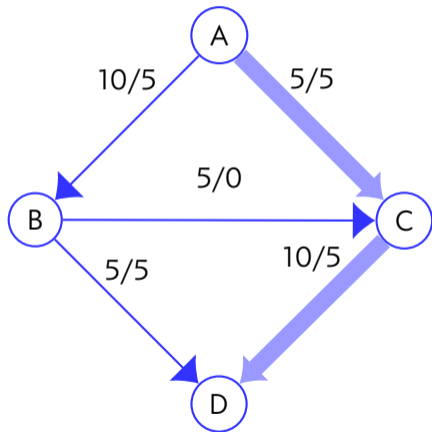
A simple example



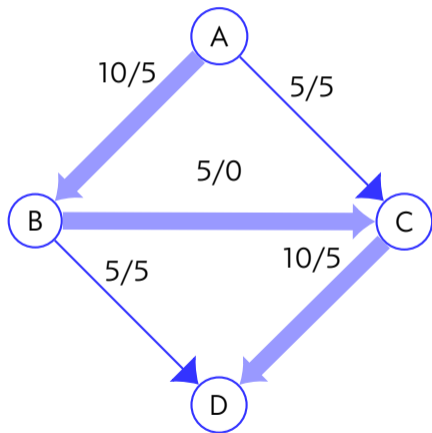
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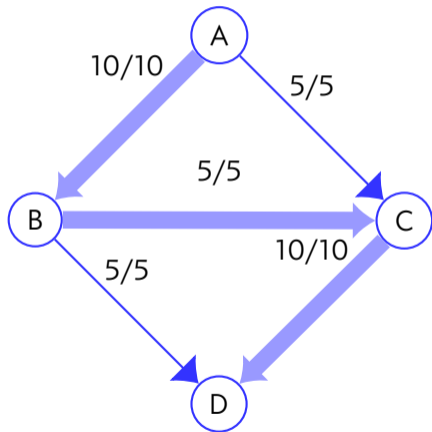
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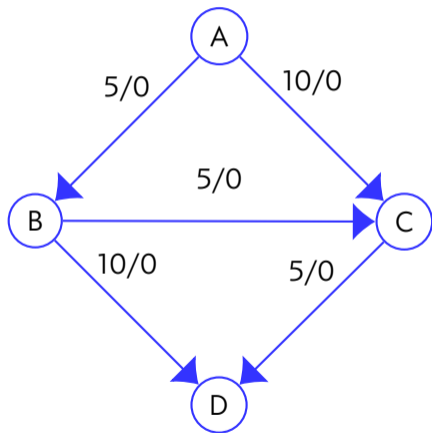
A simple example



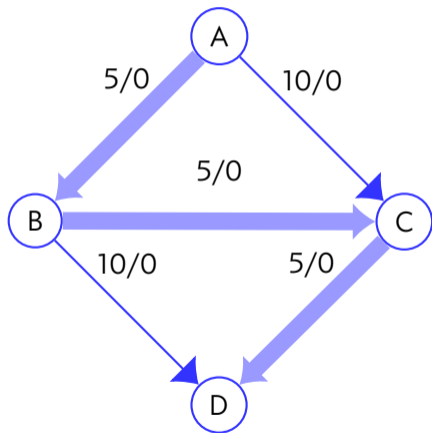
A simple example



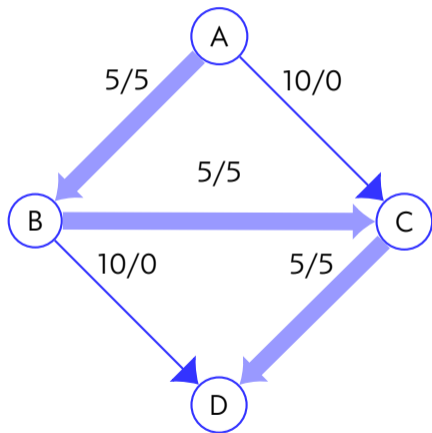
A second example



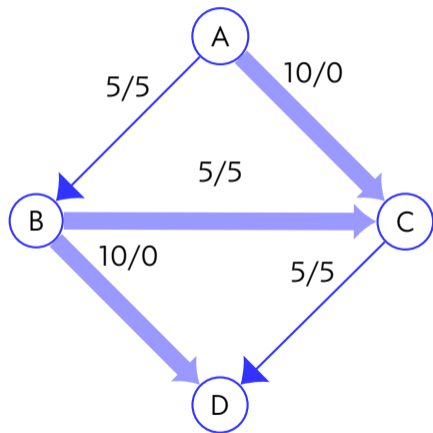
A second example



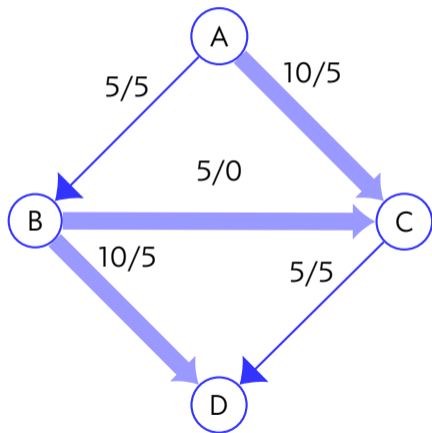
A second example



A second example



A second example



Implementation

```
// Stolen from Competitive Programming 3  
// global variables  
int res[MAX_V][MAX_V], mf, f, s, t;  
vi p; // p stores the BFS spanning tree from s  
  
// traverse BFS spanning tree from s->t  
void augment(int v, int minEdge) {  
    if (v == s) {  
        f = minEdge;  
        return;  
    } else if (p[v] != -1) {  
        augment(p[v], min(minEdge, res[p[v]][v]));  
        res[p[v]][v] -= f;  
        res[v][p[v]] += f;  
    } }  
}
```

Implementation, 2

```
mf = 0;
while (1) {// O(VE^2) (actually O(V^3 E) Edmonds Karp's algorithm
    f = 0;
    vi dist(MAX_V, INF); dist[s] = 0; queue<int> q; q.push(s);
    p.assign(MAX_V, -1);
    while (!q.empty()) {
        int u = q.front(); q.pop();
        if (u == t) break; // stop when we reach sink t
        for (int v = 0; v < MAX_V; v++)
            if (res[u][v] > 0 && dist[v] == INF)
                dist[v] = dist[u] + 1, q.push(v), p[v] = u; }
    augment(t, INF);
    if (f == 0) break; // we cannot send any more flow
    mf += f;
}
```